

# APPLICATIONS OF RELATIVISTIC QUANTUM $m$ THEORY: THE RADIATIVE CORRECTIONS

by

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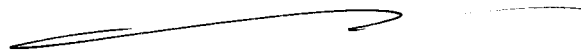
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## ABSTRACT

Relativistic quantum  $m$  theory is used to calculate and compute the radiative corrections, exemplified by the anomalous  $g$  factor of the electron and the Lamb shift in atomic hydrogen. In this way it is shown that the well known radiative corrections are the result of  $m$  space, the most general spherically symmetric space. The radiative corrections can be expressed in terms of the  $m$  parameter of this space, and show that energy is available in the  $m$  space.

Keywords: ECE unified field theory,  $m$  theory, radiative corrections.

UFT 429



## 1. INTRODUCTION

In recent papers of this series {1 - 41} the  $m$  theory has been developed in classical and quantum mechanics. This means that classical and quantum mechanics have been developed in the most general spherically symmetric space, characterized by the  $m$  function. In the preceding paper UFT428, relativistic quantum  $m$  theory was used to show that the radiative corrections can be described by the nature of  $m$  space. In Section 2 the anomalous  $g$  factor of the electron and the Lamb shift are considered within the context of relativistic quantum  $m$  theory. It is shown that the electron  $g$  factor is the result of a given  $m$  function, and the spin orbit interaction in relativistic quantum  $m$  theory is changed in detail by the  $m$  function.

This paper is a brief synopsis of detailed calculations in the Notes accompanying UFT429 on [www.aias.us](http://www.aias.us). Notes 429(1) and 429(2) develop methods of calculation of the  $g$  factor of the electron, and develop the theory of the vacuum particle first given in UFT338, giving the  $m$  theory of the mass of the universe. Note 429(3) develops the relativistic quantum  $m$  theory of spin orbit interaction, showing that  $m$  space changes the spin orbit energy levels of the Dirac equation, producing the possibility of a Lamb shift. Self consistently, the latter has already been derived using the spin connection of ECE2 theory.

Section 3 is a computational and graphical analysis using the hydrogenic wavefunctions in the first approximation. Expectation values are computed with the  $m$  function.

## 2. CALCULATION OF THE RADIATIVE CORRECTIONS

As shown in complete detail in Note 429(1) the  $g$  factor of the electron in Dirac theory is exactly two, and is calculated from the Zeeman hamiltonian:

$$H_2 \psi = i \frac{e \hbar}{2m} \underline{\sigma} \cdot \underline{\nabla} \underline{\sigma} \cdot \underline{A} \psi + \dots \quad - (1)$$

Here  $\psi$  is the wavefunction,  $-e$  is the charge on the electron,  $m$  is the mass of the electron,  $\hbar$  is the reduced Planck constant and  $\underline{A}$  the vector potential. Dirac defined the magnetic field by:

$$\underline{B} = \underline{\nabla} \times \underline{A}. \quad - (2)$$

In this theory the Bohr magneton is defined by:

$$\mu_B = \frac{e \hbar}{2m} \quad - (3)$$

and the spin angular momentum by:

$$\underline{S} = \frac{\hbar}{2} \underline{\sigma} \quad - (4)$$

with the property:

$$S \psi = m_s \hbar \psi. \quad - (5)$$

It follows that:

$$H_2 \psi = 2 g_B \mu_B m_s \psi \quad - (6)$$

and the electron  $g$  factor is the factor two appearing in this well known equation.

In relativistic quantum theory the hamiltonian (1) is changed to:

$$H_2 \psi = i \frac{e \hbar}{2m} \underline{\sigma} \cdot \underline{\nabla} \frac{1}{m(r)} \underline{\sigma} \cdot \underline{A} \psi + \dots \quad - (7)$$

where  $m(\sqrt{\quad})$  is the  $m$  function of the  $m$  space. In general  $m$  is a function of  $r$ . Using the

Leibnitz Theorem:

$$H_2\psi = i\frac{e\hbar}{2m} \left( \frac{1}{m(r)^{1/2}} \underline{\sigma} \cdot \underline{\nabla} \underline{\sigma} \cdot \underline{A} + \underline{\sigma} \cdot \underline{\nabla} \left( \frac{1}{m(r)^{1/2}} \right) \underline{\sigma} \cdot \underline{A} \right) \psi \quad (8)$$

and using the Pauli algebra:

$$\underline{\sigma} \cdot \underline{B} \underline{\sigma} \cdot \underline{A} = \underline{B} \cdot \underline{A} + i \underline{\sigma} \cdot \underline{B} \times \underline{A} \quad (9)$$

the real and physical part of the hamiltonian is:

$$\begin{aligned} H_2\psi &= \frac{e\hbar}{2mm(r)^{1/2}} \underline{\sigma} \cdot \underline{\nabla} \times \underline{A} \psi - \frac{e\hbar}{2m} \underline{\sigma} \cdot \underline{\nabla} \left( \frac{1}{m(r)^{1/2}} \right) \times \underline{A} \psi \\ &= - \left( \frac{2}{m(r)^{1/2}} \right) \left( \frac{e\hbar}{2m} \right) m_s B_z \psi - 2 \left( \frac{e}{2m} \right) \underline{\sigma} \cdot \underline{\nabla} \left( \frac{1}{m(r)^{1/2}} \right) \times \underline{A} \psi \quad (10) \end{aligned}$$

Therefore the anomalous  $g$  factor of the electron is:

$$g = \frac{2}{m(r)^{1/2}} \quad (11)$$

Experimentally:

$$g = 2.002319314 \quad (12)$$

so:

$$m(r) = 0.99942068 \quad (13)$$

The relativistic quantum  $m$  theory gives the  $g$  factor of the electron to any accuracy. It is seen that  $m(\sqrt{\quad})$  is very close to unity, so the space is close to being the Minkowski spacetime in which Dirac's theory of the electron was developed.

The theory of the anomalous g factor can also be developed following the methods of UFT338, in which the vacuum particle of ECE2 theory was inferred. As shown in Note 429(2) the classical hamiltonian of m theory in frame  $(r_1, \phi)$  is:

$$H = m(r_1) \gamma m c^2 + \bar{U} \quad - (14)$$

where the total relativistic energy is:

$$E = m(r_1) \gamma m c^2 \quad - (15)$$

and where  $\gamma$  is the generalized Lorentz factor of m theory. Here U is the potential energy.

In immediately preceding papers it is shown that:

$$E^2 = m(r_1) (c^2 p_1^2 + m^2 c^4) \quad - (16)$$

It follows as in Note 429(2) that:

$$H = \frac{c^2 p^2}{E + m(r)^{1/2} m c^2} + m(r)^{1/2} (m c^2 + \bar{U}_0) \quad - (17)$$

where

$$\bar{U}_0 = -\frac{e^2}{4\pi \epsilon_0 r} \quad - (18)$$

is the potential energy due to the interaction of the electron and proton in an H atom.

Now develop the de Broglie / Einstein energy equation of UFT338 to m space

$$E = m(r) \gamma m c^2 = \hbar \omega \quad - (19)$$

It follows that:

$$H = \frac{p^2}{m \left( \frac{\hbar \omega}{m c^2} + m(r)^{1/2} \right)} + m(r)^{1/2} (m c^2 + \bar{U}_0) \quad - (20)$$

For:

$$m(r) = 1 \quad - (21)$$

Eq. ( 20 ) reduces to the theory of UFT338:

$$H = \frac{p^2}{m \left( \frac{\hbar \omega}{mc^2} + 1 \right)} + mc^2 + U_0 \quad - (22)$$

Q. E. D.

In the SU(2) basis Eq. ( 20 ) is

$$H = \frac{1}{m} \underline{\sigma} \cdot \underline{p} \frac{1}{\left( \frac{\hbar \omega}{mc^2} + m(r) \right)^{1/2}} \underline{\sigma} \cdot \underline{p} + m(r)^{1/2} (mc^2 + U_0) \quad - (23)$$

and in the presence of a magnetic field:

$$H = \frac{1}{m} \underline{\sigma} \cdot (\underline{p} - e \underline{A}) \frac{1}{\left( \frac{\hbar \omega}{mc^2} + m(r) \right)^{1/2}} \underline{\sigma} \cdot (\underline{p} - e \underline{A}) + m(r)^{1/2} (mc^2 + U_0) \quad - (24)$$

On quantization it is found that:

$$H \psi = -2 \frac{e}{m} \left( \frac{1}{\left( \frac{\hbar \omega}{mc^2} + m(r) \right)^{1/2}} \right) \underline{S} \cdot \underline{B} \psi + \dots \quad - (25)$$

as in Note 429(2). The g factor of the electron is defined as:

$$H \psi = -g \frac{e}{2m} \underline{S} \cdot \underline{B} \psi \quad - (26)$$

So from Eqs. ( 25 ) and ( 26 ):

$$\frac{g}{2} = \frac{2}{\left( \frac{\hbar \omega}{mc^2} + m(r) \right)^{1/2}} \quad - (27)$$

and

$$g = \frac{4}{\frac{\hbar \omega}{mc^2} + m(r)^{1/2}} \quad - (28)$$

In the limit:

$$m(r) = 1 \quad - (29)$$

it follows that:

$$g = \frac{4}{\frac{\hbar \omega}{mc^2} + 1} \quad - (30)$$

and for the rest electron:

$$\hbar \omega_0 = mc^2 \quad - (31)$$

so the Dirac g factor follows:

$$g = 2 \quad - (32)$$

Q. E. D.

The Dirac g factor is a limit of m theory.

For the rest electron with finite  $m(r)$ :

$$g = \frac{4}{1 + m(r)^{1/2}} \quad - (33)$$

and using the observed g factor ( 12 ) it is found that:

$$m(r) = 0.99884 \quad - (34)$$

which is close to the  $m(r)$  given in Eq. ( 13 ).

The Lamb shift in atomic H can be calculated from the spin orbit hamiltonian. In

Dirac theory (Note 330(1)) this is given by:

$$H\psi = \frac{1}{4m^2 c^2} \underline{\sigma} \cdot \underline{p} U \underline{\sigma} \cdot \underline{p} \psi \quad - (35)$$

and as shown in all detail in Note 429(3) the hamiltonian (35) gives:

$$\begin{aligned} H\psi &= \frac{e^2}{8\pi c^2 \epsilon_0 m^2 r^3} \underline{S} \cdot \underline{L} \psi \quad - (36) \\ &= \frac{e^2}{16\pi^2 c^2 \epsilon_0 m^2 r^3} \left( J(J+1) - L(L+1) - S(S+1) \right) \psi \end{aligned}$$

where  $\epsilon_0$  is the vacuum permittivity. The total angular momentum quantum number  $J$  is defined by the Clebsch Gordan series:  $L - S, \dots, L + S$ .

$$\begin{aligned} \text{The expectation value of } H \text{ is evaluated with:} \\ \left\langle \frac{1}{r^3} \right\rangle = \int \psi^* \frac{1}{r^3} \psi d\tau = \left( \frac{Z}{a_0} \right)^3 \frac{1}{n^3 L(L + \frac{1}{2})(L+1)} \end{aligned} \quad - (37)$$

where  $a_0$  is the Bohr radius, and in atomic H:

$$Z = 1 \quad - (38)$$

Here  $n$  is the principal quantum number. So the energy levels of atomic H are given by:

$$\left\langle H_{S_0} \right\rangle = \frac{e^2 \hbar^2}{16\pi c^2 \epsilon_0 m^2 a_0^3} \left( \frac{J(J+1) - L(L+1) - S(S+1)}{n^3 L(L + \frac{1}{2})(L+1)} \right) \quad - (39)$$

where:



$$J = L - S, \dots, L + S \quad (40)$$

in which  $L$  is the orbital angular momentum quantum number and  $S$  the spin angular momentum quantum number.

In this Dirac theory it is well known that there is no Lamb shift, there is no difference between the energy of  $^2P_{1/2}$  and  $^2S_{1/2}$ , contradicting experiment.

In m theory denote:

$$U_1 = \frac{U}{m(r)^{1/2}} \quad (41)$$

so the real part of the relevant hamiltonian is:

$$Re H_{so} \psi = \frac{e\hbar}{4m^2c^2} \underline{\sigma} \cdot \underline{\nabla} U_1 \times \underline{p} \psi \quad (42)$$

Using the Leibnitz theorem:

$$\underline{\nabla} U_1 = \underline{\nabla} \left( \frac{U}{m(r)^{1/2}} \right) = \frac{1}{m(r)^{1/2}} \underline{\nabla} U + U \underline{\nabla} \left( \frac{1}{m(r)^{1/2}} \right) \quad (43)$$

and it follows that:

$$Re H_{so} \psi = \frac{e^2 \hbar}{16\pi \epsilon_0 m^2 c^2 r^3 m(r)^{1/2}} \underline{\sigma} \cdot \underline{L} \psi + \frac{e\hbar}{4m^2c^2} U \underline{\sigma} \cdot \underline{\nabla} \left( \frac{1}{m(r)^{1/2}} \right) \times \underline{p} \psi \quad (44)$$

Therefore the energy levels of the H atom are:

$$\langle H_{so} \rangle = \frac{e^2 (J(J+1) - L(L+1) - S(S+1))}{16\pi c^2 \epsilon_0 m^2} \left\langle \frac{1}{r^3 m(r)^{1/2}} \right\rangle + \dots \quad (45)$$

where

$$\left\langle \frac{1}{r^3 m(r)^{1/2}} \right\rangle = \int \psi^* \frac{1}{r^3 m(r)^{1/2}} \psi d\tau \quad (46)$$

The appearance of  $m(r)^{1/2}$  in the expectation value, Eq. (46), may already be sufficient to give the Lamb shift and to lift the degeneracy of  $^2P_{1/2}$  and  $^2S_{1/2}$ . If not, additional terms may be used in Eq. (44).

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