

Addendum for Note 249(2)

If: $\underline{A} = \frac{1}{2} \underline{B} \times \underline{r} \quad - (1)$

then we must have:

$$(\underline{r} \cdot \underline{\nabla}) \underline{B} - (\underline{\nabla} \cdot \underline{B}) \underline{r} = \underline{0} \quad - (2)$$

Consider rotating magnetic field:

$$\underline{B} = \frac{B^{(0)}}{\sqrt{2}} (\underline{i} - i\underline{j}) e^{iat} \quad - (3)$$

then: $\underline{\nabla} \cdot \underline{B} = 0 \quad - (4) \quad \checkmark \checkmark$

and
$$(\underline{r} \cdot \underline{\nabla}) \underline{B} = \left(x \frac{\partial}{\partial x} + y \frac{\partial}{\partial y} + z \frac{\partial}{\partial z} \right) \underline{B} = \underline{0} \quad - (5) \quad \checkmark \checkmark$$

The vector potential is:

$$\begin{aligned} \underline{A} &= \frac{1}{2} \underline{B} \times \underline{r} = \frac{1}{2} \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ 1 & -i & 0 \\ x & y & z \end{vmatrix} \frac{B^{(0)}}{\sqrt{2}} e^{iat} \\ &= \frac{B^{(0)}}{2\sqrt{2}} e^{iat} \left(-z(1+i)\underline{j} + \underline{k}(y - ix) \right) \end{aligned} \quad - (6)$$

So computer algebra can be used to rework note 249(2) w/ $\underline{A}$'s vector potential.
